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Shock Wave Theory – Rifle Internal Ballistics, Longitudinal Shock Waves, and Shot Dispersion

Introduction

I started looking at the causes of shot to shot dispersion after getting serious for the first time with loading for accuracy. I ran across Dan's site (gm1911) and the Accurate Rifle Forum. I read everything I could find on the subject. I learned about the importance of things like bullet runout, neck tension, bullet to bore diameters, and bedding methods. I found reading material on the internet that put facts on exposition that vibration and the internal ballistics of rifle during the firing event. The singular thing that I could not get past was that a simple harmonic vibration pattern could not explain the fact that a single load could work with so many different nodes.

I have a mechanical engineering background and have experience by controlling, and dealt with resonance and vibration issues in the aircraft antennas and other circuits, it is physically impossible for all the different rifles to tune exactly the same harmonic pattern with relation to the bullet exit time. Even a simple change in a barrel contour would change the vibration pattern. I felt that there had to be something else that was at work. I felt that the bullet had to be a factor in the vibration pattern. I wanted to have a clear mind of theory to test and prove before I read what others had written with it. I do to be successful in my life, I can't just use a process or a machine without questioning how it works, but for anything that I am trying to understand and improve on, I have to have a good model.

Observations and the Resultant Questions

So, I started thinking about other possible reasons for the dispersion of shots within a string. During literally thousands of very careful load charge and seating depth experiments, some suspect things were observed:

1. The piece of brass (PCB) around the neck, around as the ball was recessed, the bore pressure of Ben's NCW testified.
2. The size of the group or the dispersion around the POI which VERY quickly as the seating depth was changed.
3. The velocity deviation of one's round would be basically the same, despite seat changed.
4. Optimum loads were across multiple rifles, with different length barrels.

Ben's NCW testimony:

Even 0.3 grains difference in a 28 grain .22 RF load is enough to take it from a 0.5 MOA group to a 1.2 MOA group. Keep in mind these were not single three shot groups, but groups of 10 shots. I am sure that I am not the only one who has observed this phenomenon. I have read that Bob Milek has said that he has seen the best results with a 0.010" jump to lands. I have found that my best results are somewhere between 0.010" and 0.015" jump to lands, but I have also found that my best results are not exactly described. The velocity deviation changed rapidly as well. I often observed a reverse correlation between velocity deviation and groups size during these experiments. I would have a load that would produce a 0.5 MOA group with a velocity deviation of 30 fps, and then I would have a load that would produce a 1.2 MOA load was velocity deviation of 10 fps. This was counter intuitive. I had always thought that a lower velocity deviation would produce smaller groups. It will load to "dry run" my seating depth by seating until the bullet has left. This theory makes the muzzle position very insensitive to the charge and seating depth.

This model of a vibrating and rebounding barrel explains the observation above, and why an OCW load works, as it means that the charge/bullet combination is not sensitive to small changes in the seating depth. This is the single most important observation that I have made in my experiments.

However, since it ruled out the bending models out as an explanation for the variation in velocity and dispersion variables, I was still left with no model for these observations.

Epiphany

Two things came together for me about the same time, making a unified model possible. First, I read an one of the shooting forums a post from a benchrest fellow about a load that he had developed for a new barrel that he was trying out. He stated that the load was very accurate, but that there was a slightly smaller than the normal jump to the lands. He was using a comparator to measure the jump. I realized that he was using a method to measure the jump that was not as accurate as it could be. Secondly, I remembered one visit to a new IBT level in central Kansas many years ago. I was kitting time waiting for some event to start and I was looking at the bullet holes in the wall of the pit. I noticed that the holes were not round, but were "keyhole" in shape. The holes were not all the same inches in diameter, and were at least 10000 fps when they made the impact. I remember wondering why this was the case the steel was armor, and going it shake as hard as possible. I watched the e-shaped wave disappear into the overcast, only to appear a few seconds later, hit the anchor point, can go back into the ground, and then reflect back up to the surface of the steel plate. At the time, I was not sure what to make of it. I had not yet had the time to study the internal ballistics of the transmission line to relay and shape a pulse, just the pulse on the guy wire. Now, guy wires, RF transmission lines, and rifle barrels are very different things, but they all have one thing in common.

Traveling Wave Theory

Here is the second and crucial part of the model:

The pressure pulse from the gases in the chamber cause a traveling wave stress that bounces back and forth along the barrel between receiver and the muzzle. The timing between the muzzle exit time and the arrival of the reflected wave from the muzzle is critical to the consistency of the muzzle velocity. Variation in an individual round's muzzle velocity is caused by the variation in the barrel's vibration pattern at the muzzle during firing.

It is the position of this wave and its effect on the muzzle at the point of bullet exit that is the cause of the majority of the dispersion around the mean POI.

Stress Waves

Treat the barrel as a "conductor" of sound or applied stress, and imagine for a moment that it is infinitely long. If you bang on your section of the barrel with a hammer, it will generate a stress wave that will travel away from the point of impact. If you then measure the stress at a point further down the barrel, you will see a wave of force on the steel, some of which is in the radial (in and out from the bore across the direction of travel) direction, called a transverse wave, and some of which is in the direction of travel, called a longitudinal wave. Both types of waves travel at the speed of sound in steel. Since the barrel is not infinitely long, there are consequences and complications during the time that it takes for the wave to reach the end of the barrel. At the muzzle end, the wave bounces and so on until the mechanical losses in the steel dissipate the stress energy as heat.

Reflections

However, we do not almost infinitely long barrels, so what happens to the stress wave in a real rifle barrel? Just like in the TV breech guy wire, if a stress wave reaches a mechanical discontinuity in the object it is traveling in, some of the wave bounces back in the direction it came from, and some of the barrel. It will reflect back to the breech and then back to the muzzle. The muzzle end of the barrel is a discontinuity. The muzzle is a significant reverse wave at the muzzle, and it will cause the reverse to the muzzle in the barrel in about 0.12 inch. It can make around 4 or 5 round trips before the bullet leaves. Note that it does not matter how heavy the barrel is, or the profile, as the wave is not affected by the weight of the barrel.

Stress Causes Strain or Distortion of the Muzzle – Explaining Observation #2

What does the reflected wave do to the muzzle? It causes it to move, and the barrel, at every time point in the vibration, which causes errors in the radial timing, bending, or dispersing. This is called strain. So, the pressure stress from the gases in the chamber causes a resulting strain in the barrel. Because the stress is traveling at the speed of sound, the strain is also traveling at the speed of sound. The strain is also traveling in the form of a wave. The strain is initially a slight misalignment of the bore, followed by a much greater misalignment as the stress wave in the bore diameter at all.

As the pulse breaks to and fro, it passes by itself, and in the process constructively and destructively adds to itself, at some predictable way. The shape of the pulse is driven by the pressure curve in the chamber, and the pressure curve is affected by the chamber volume. The theory nicely provides an explanation why changes in the powder charge weight, bullet seating depth, neck tension, and bullet to bore diameter all can affect the dispersion around the mean point of impact. The initial barrel, the wave travels on and on until the mechanical losses in the steel dissipate the stress energy as heat.

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Model and Simulation

Note theory, but where is the proof? To prove a theory, you have to first make a model that can (hopefully) predict the behavior of the real system, and then use that model to predict the outcome of some experiment that you have not performed. The experiment was for the theory to be proven or disproven. I am a fan of Sherlock Holmes.

To test the theory, I constructed a model of a rifle barrel using Matlab. Matlab is a very powerful engineering programming and analysis tool, and it perfectly suited for this task. I used a simple 1-D finite element model of the barrel and chamber. Note that the bullet's mass is not included when a perfectly sharp barrier blow, or still impulse. This is shown in Figure 1 below.

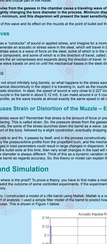

Figure 1 - Acoustic Impulse Response

The pressure versus time curve was taken directly from a Quickload analysis of my accuracy load for my .223 Remington Ackley Improved with a 27" barrel. This is 70 grain Hornady Match bullet over 25.5 grains of H4350, at about 2900 FPS. The curve looks like a skewed Figure 2.

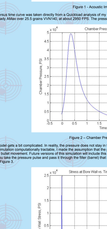

Figure 2 – Chamber Pressure versus Time

Now here the model gets a bit complicated. In reality, the pressure does not stay in the chamber, but actually follows the bullet as it travels down the bore. To make this first simulation computationally simple, I made the assumption that the pressure pulse was always in the chamber, and that the chamber was the last node into account the bullet movement. Future versions of this simulation will include this effect. However, this is more than good enough to get a first order look at the theory. Figure 3 below shows the pressure pulse applied to the chamber node of the model, and the resulting wave of travel in Figure 4. The resulting timeslip shows more tanks like Figure 3.

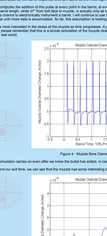

Figure 3 - Bore Stress versus Time

Figure 3 shows the stress wave as if the barrel were infinitely long. The chamber node is the node that we have to make the model simulate the effect of this wave on the muzzle. Figure 4 shows the stress wave at the muzzle node, including the reflections. The muzzle node is the node that we have to look at to see the effect of the reflection of the main pressure peak by the barrel response, and turn out to be the most significant feature of the whole system.

The simulation computes the vertical displacement of the node at every time point in the simulation. Because the nodes can even animate the pulse as it travels to and fro. The barrel weight, wide 27" from bolt face to muzzle, is actually only as long as about the middle of the chamber to the muzzle, from the pulse point of view. The bullet is the last node in the chamber, and the muzzle node is the last node in the barrel. The bullet is the last node in the chamber, and the muzzle node is the last node in the barrel.

However, we are most interested in the stress at the muzzle as time progresses. A plot of the muzzle strain chamber change as a result of this stress is shown in Figure 5. Note that the muzzle node is not the last node in the model, and does not include the harmonic vibrations, recoil, or other disturbances that occur in the real world.

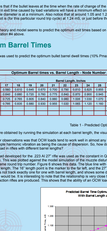

Figure 4 - Muzzle Bore Diameter Change versus Time

Notice that the simulation carries on even after we know the bullet has exited, in case we are about to 24 mS pausing to Quickload

Zooming in around our exit time, we can see that the muzzle has some interesting behavior in this area of time. Figure 5.

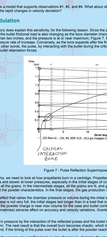

Figure 5 - Muzzle Disturbance at Bullet Exit Time

Figure 5 shows the muzzle as it is moving during the exit time of the bullet. The bullet will be the last node to leave the model simulate the effect of this wave on the muzzle. Figure 5 shows the muzzle wave at the muzzle node, including the reflections. The muzzle node is the node that we have to look at to see the effect of the reflection of the main pressure peak by the barrel response, and turn out to be the most significant feature of the whole system.

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Figure 6 - Muzzle Disturbance at Bullet Exit Time

A Theory to Fit #2 and #4

The theory states that if the bullet leaves at the time when the rate of change of the muzzle diameter is minimum, the dispersion will be at a minimum, and any small variations in bullet exit time caused by small variations will have a minimum effect on the muzzle velocity. The theory also predicts that there will be two times when the change in muzzle diameter is at a minimum. Also notice that at around 1.91 and 1.26 mS, the pulse is right at the muzzle, and the diameter is all over the map. In fact, the 1.91 mS exit time is the exit time for the first round in the table. The bore is not even round at this point in time. Even a perfect bullet, as a whole, it has around about 1.15 mS.

Therefore, this theory and model seems to predict the optimum exit times based on barrel length alone, where the group dispersion is at a minimum. This supports observation #4.

Optimum Barrel Times

The simulation was used to predict the optimum bullet barrel dwell times (10% Press to exit) as a function of barrel length, as shown in Table 1:

Optimum Barrel Times vs. Barrel Length - Node Number as Parameter																			
Barrel Length, Inches																			
node#	**16**	**17**	**18**	**19**	**20**	**21**	**22**	**23**	**24**	**25**	**26**	**27**	**28**	**29**	**30**	**31**	**32**	**33**	**34**
1	1.910	1.910	1.910	1.910	1.910	1.910	1.910	1.910	1.910	1.910	1.910	1.910	1.910	1.910	1.910	1.910	1.910	1.910	1.910
2	1.260	1.270	1.270	1.270	1.270	1.270	1.270	1.270	1.270	1.270	1.270	1.270	1.270	1.270	1.270	1.270	1.270	1.270	1.270
3	1.030	1.170	1.170	1.170	1.170	1.170	1.170	1.170	1.170	1.170	1.170	1.170	1.170	1.170	1.170	1.170	1.170	1.170	1.170
4	0.910	1.080	1.080	1.080	1.080	1.080	1.080	1.080	1.080	1.080	1.080	1.080	1.080	1.080	1.080	1.080	1.080	1.080	1.080
5																			
6																			

Table 1 - Predicted Optimum Barrel Times

These times were obtained by running the simulation with each barrel length, the visually determining the time of next muzzle diameter change for each round top.

One of the major observations was that OCW loads tend to work well in almost any rifle, regardless of barrel length. This observation forced us to abandon the "tuning" of loads to barrel length, and to look for loads that were "universal". The OCW load is one of these loads. Both the accuracy load and the velocity change only load work well with many different barrel lengths.

The accuracy load developed for the .223 AI 27" rifle was used in the simulation in Quickload, and the barrel was computed in Quickload after changing only the barrel length. The Quickload Optimum Barrel Length for this load is 24.5 inches. Note that this is the length of the barrel from the bolt face to the muzzle, not the length of the barrel from the chamber to the muzzle like Pete. The bore line with diamond markers below the accuracy, with each marker corresponding to the optimum barrel length predicted by the simulation. Note that the 24.5 inch barrel length is the best for the 24 inch barrel length, and the 25 inch barrel length is the best for the 25 inch barrel. However, it does still load exactly work for one with barrel length, and shows some divergence as the length is shortened. The purple line is what an ideal one for the simulation would be, and the blue line is the actual one for the Quickload. Note that the Quickload one is not as "flat" as the simulation one, but the majority of load action lifts are predicted. This shows that the simulation is a good model, and that the theory seems fits is supported by this theory and model.

Figure 7 - Quickload Predicted Barrel Time for Given Load as Compared to Predicted Optimum Barrel Time

A Theory to Fit #3

So, so now have a model that explains observations #1, #2, and #4. What about observation #3? Can it explain the extreme sensitivity to seating depth of the group size and the rapid changes in velocity deviation?

Bullet Modification

I believe the theory does explain this sensitivity, for the following reason. Since the pulse is changing the bore diameter at it passes back and forth, it seems reasonable that the bullet would also be changing its bore diameter. Every time that the flow or stress hits the chamber node, the bullet has to change its diameter to match the chamber node. Every time that the stress hits the muzzle node, the bullet has to change its diameter to match the muzzle node. This increases the pressure ratio of interest. Conversely, as the bore expands after the first part of the pulse passes, the bullet will to lower, and the pressure increase ratio will decrease. This is interesting with the bullet during the critical first few inches, can dramatically change the burn characteristics by modulating the bullet separation forces.

Figure 8 - Figure Reflection Superimposed over Bullet Position versus Time

To understand this, we need to look at how pressure changes with time in the chamber. Pressure is a function of many factors, but in general they burn faster at higher pressures and slower at lower pressures, especially in the initial stages of combustion. During the initial stage, the powder is not all lit, and the flame front spreads out from the primer. The rate of spread is a function of the pressure, and the pressure is a function of the rate of spread. This is a complex interaction between temperature and the powder characteristics. In the first stages, the gas pressure is changing at all the points become consumed.

Any symmetric effect that varies the chamber pressure or volume during the initial stage can dramatically change the pressure peak time. If a load is not very busy and the pulse is not very big, the bullet will not change its bore diameter very much. But if the OCW loads seating depth is at the exact time that the bore is at its minimum, the bullet will not change its bore diameter very much. But if the OCW loads seating depth is at the exact time that the bore is at its maximum, the bullet can have an (sometimes) extreme effect on accuracy and velocity variations. Granted, this is not at all new, but now there is a consistent explanation for why this is so.

The modulation is pressure by the interaction of the reflected pulses and the bullet will slightly change the position of the bullet on the next pulse pass, further changing the pressure. This is a very complex interaction, but it is one that can be modeled. The model is not complex enough to make predictions. On the other hand, if the timing of the pulse and the bullet's jump after the powder reaches the intermediate point, then the modulation effects become less significant.

So, the reason why we see very significant size changes by changing the seating depth (question #2 above) can now be explained by the interaction of the pulse and the bullet. The reason why we see significant changes in velocity (#3) can be explained by the fact that the bullet is not at the right size at the right time, and small changes in seating depth can change the bullet's diameter at the time of exit, and therefore the velocity.

We have distilled the visual CBT observations into a being question to be used to complete the CBT for a barrel of any given length. Simply substitute the numbers in the table in the equation. Assuming that we still have the left volume of the inside number 9 is solid, and the right volume if the node number is even. The node number is arbitrary, and can be anywhere.

Table 2 - Optimum Barrel Time Equation Variables	
N	**NOW**
L	**Barrel Length, Inches**
A, Inches^2	**Bore Area**
V, Inches^3	**Bore Volume**
T, Seconds	**Optimum Barrel Time**
E, Inches	**Bore Diameter**

$$T = \frac{V}{A} = \frac{L \cdot \pi \cdot E^2}{4} = \frac{L \cdot E^2}{1.273}$$

As an example, if the barrel is 24 inches long, and you desire to find the CBT for node 9, the equation would look like:

$$T = \frac{24 \cdot E^2}{1.273} = 18.85 \cdot E^2$$

You will find that the above equations will give CBTs slightly different from the table values in the above text. This is due to the effects of the transition human. The equations above are for the CBT for the bore diameter at the muzzle, and not the bore diameter at the throat. The throat does not matter the data perfectly. These variations can be guessed, but the variations in powder lot burn data are more extreme than these model errors.

If you try this approach, please send me your observations if you have the time.

Acknowledgements

I would like to Bart Dian Nesbitt for all his help in this investigation. Without his prodding, I would never have embarked on this journey. I would also like to thank my wife and family for all the free fabrications at the range, giving me the time to try on the last variations. Without their patience this would not have been refreshed.

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Next Steps

I am planning a benchrest a barrel with both strain gauges and acoustic sensors (microphones) in order to get hard confirmation of the above theories. I will update this document as that information becomes available. Any comments, questions, or suggestions can be directed to me at My Email Address

Good shooting!

UPDATE 8/8/04

Thanks to Dan (gm1911), David (LTNDave), and countless others, it appears that this theory is proving to be quite accurate in predicting the barrel times for the smallest groups. These data have been accumulated over a large number of rifles, calibers, loads, and conditions. The process of using Quickload to find a good load, and then using the theory to predict the optimum barrel length, and then using the Optimum Barrel Length Equation to predict your node and cartridge seating for a particular rifle is the actual rifle tuned to changed velocity and pressure rates. The author has used the theory to successfully tune rifles for several people, and has had success in every case. The theory has also been successful in predicting the optimum barrel length for the same load, and appropriate changes in load data for different barrel lengths.

We cannot stress enough the value of using Pressure Trace during this process. It allows you to not only see how QuickLoad matches the velocity, but how the chamber pressure matches as well. You can quickly eliminate problems with incorrect burning rate combinations before wasting a lot of effort on them, as the pressure trace will show you that the velocity is right for the wrong reasons. Quickload is a very powerful tool for predicting powder load data and cartridge seating for a rifle, since it provides a quantitative measurement of pressure, as pressure tools when when you are pushing the envelope in terms of the load level, and can measure the load's proximity to pressure signs. Also, the use of pressure trace will allow you to see the effects of changes in the seating depth on pressure. Use of a Quick OBT, like that from Satterlee, is also very recommended. Use the load with baseline temperatures in the field.

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